

## Modeling auditory cortical processing as an adaptive chirplet transform<sup>☆</sup>

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### Abstract

Recent evidence suggests that (a) auditory cortical neurons are tuned to complex time-varying acoustic features, (b) auditory cortex consists of several fields that decompose sounds in parallel, (c) the metric for such decomposition varies across species, and (d) auditory cortical representations can be rapidly modulated. Past computational models of auditory cortical processing cannot capture such representational complexity. This paper proposes a novel framework in which auditory signal processing is characterized as an adaptive transformation from a one-dimensional space into an  $n$ -dimensional auditory parameter space. This transformation can be modeled as a chirplet transform implemented via a self-organizing neural network. © 2000 Elsevier Science B.V. All rights reserved.

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### 1. Introduction

How networks of cortical neurons represent sound is poorly understood. Although electrophysiological studies have demonstrated that firing patterns in specific neural regions can often be predictably correlated with particular sound features, the underlying neural codes that give rise to such correlations remain unclear. Recently, there have been an increasing number of attempts to develop signal processing models of audition [16,26,27]. The motivation behind these efforts is the hope that current

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computational techniques can provide insight into how neural circuits encode representations of acoustic events. In the current paper, we propose a heuristic model of auditory cortical processing based on recently described signal transformation techniques and self-organizing neural networks. This model encapsulates much of what is currently known about the response properties of auditory cortex. These properties include:

- Complex patterns of sound feature selectivity [8,16,22,36].
- Species-specific signal decomposition [28,31,33].
- Dynamic modulation of response characteristics [3,5,10–12,37].
- Systematic topography of cortical sensitivities [1,30].

Our intention is that the model be flexible enough that it can be used to describe how sounds are cortically encoded in any mammalian species.

Past computational models of auditory cortical processing have focused primarily on emulating neural sensitivities measured from individual neurons in a particular species. For example, Suga [32,33] described auditory processing in bats as parallel, hierarchical cross correlation. He modeled individual neurons as delay lines, multipliers, logical gates, and filters that decomposed incoming signals into functionally relevant temporal and/or spectral features. Processing in bats has also been modeled as (1) spectrographic cross correlation, followed by transformation into auditory parameters [29], (2) transformation from neural spike trains into a spatial array of delay sensitive units [25,26], and (3) binaural recognition of waveform envelopes [17]. Perhaps the most sophisticated models of auditory cortical processing developed to date characterize response sensitivities in ferrets [16,34,35]. Wang and Shamma [35] modeled auditory cortical neurons as perceptrons with weight vectors corresponding to the neural sensitivities of ferrets. These sensitivities were found to be analogous to a topographically organized wavelet transform. Attempts have also been made to model auditory processing in humans [4,7,18]. These models tend to focus on known psychophysical sensitivities (e.g., timbre and pitch perception) rather than electrophysiological response properties.

The standard approach to modeling auditory cortical processing has been to start with a general signal processing model (e.g., Fourier or wavelet transforms), and then to add on specialized processing components (e.g., matched filters) to reflect species-specific sensitivities. This approach is problematic because (1) the customization needed to describe cortical sensitivities in any given species can only be retrospectively determined (i.e., the models are not predictive), (2) most evidence suggests that auditory cortical sensitivities reflect the particular needs of individuals faced with species-specific ecological and biological constraints, rather than generic acoustic signal processing strategies, and (3) experience-dependent adaptations in auditory processing are not considered. A more flexible framework is needed to adequately characterize the full range of auditory cortical sensitivities observed in mammals. Our approach involves first finding a transform general enough to describe cortical signal decomposition across all mammals. This transform is then mapped onto an unsupervised neural network that can learn to efficiently code acoustic events that are of functional relevance to a particular species/individual.

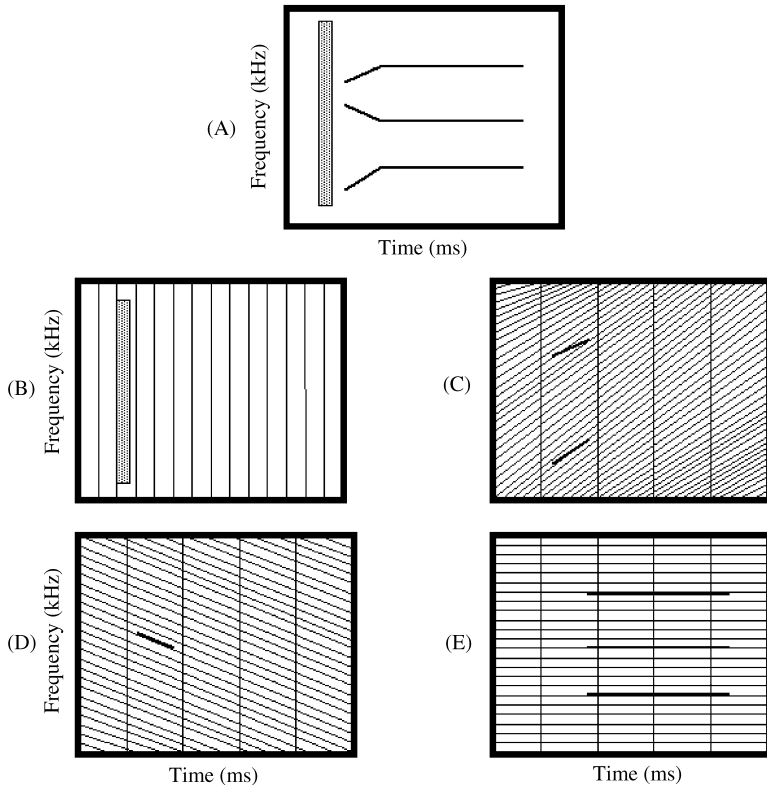


Fig. 1. An example of chirplet decomposition. (A) Idealized spectrogram of a spoken syllable (based on [32]). Dark regions of the spectrogram reflect higher spectral energy levels during short time intervals. The chirplet transform describes spectrograms such as (A) in terms of divisions of the time–frequency plane. For example, in (B) the initial broad band noise burst in the syllable (corresponding to a consonant) can be described as the third “slice” when the plane is vertically (i.e., temporally) segmented. In contrast, frequency-modulated components of the syllable (corresponding to the onset of a vowel), shown in (C) and (D) are better described in terms of divisions that segment the plane both vertically and diagonally. Finally, (E) shows that continuous frequency components are best characterized in terms of orthogonally segmented divisions. Chirplet spaces are defined based on the range of allowable divisions of the time–frequency plane. In the example above, dimensions of chirplet space correspond to the positions, sizes, and tilts of parallelograms covering the plane. Any syllable can be described in terms of a set of parallelograms that contain high concentrations of energy; each possible parallelogram corresponds to a point within the chirplet space. It is important to note that the shapes of segments are not limited to parallelograms. The basis functions chosen for the chirplet transform specify the geometry of segmentation.

## 2. Adaptive chirplets

A recently developed signal processing model, called the chirplet transform, appears to be well suited for our purposes. The chirplet transform subsumes both Fourier

analysis and wavelet analysis (as well as several other classes of time-frequency analysis) as lower dimensional subspaces in the chirplet analysis space [19–21], providing a broad framework for mapping one-dimensional sound waveforms into an  $n$ -dimensional auditory parameter space. Fig. 1 illustrates the basic structure of the chirplet transform.

The chirplet transform retains the advantages offered by time frequency and wavelet transforms, and additionally provides a natural way for characterizing the different types of processing that have been described for different auditory fields (i.e., cortical regions with systematically related response sensitivities). Each auditory field can be viewed as a processor for decomposing sounds within a particular subspace of the complete auditory parameter space. In our framework, these fields correspond either to chirplet subspaces or to chirplet spaces generated by sets of functionally relevant basis functions. Chirplet spaces are highly overcomplete (redundant) because there are an infinite number of ways to segment a time-frequency plane. Because of this overcompleteness, the same acoustic feature may be encoded multiple times. Such multiplicative, overcomplete encoding corresponds well with the overlapping, parallel signal processing pathways observed in mammalian auditory cortex [1].

The flexibility of the chirplet transform comes at the price of loose constraints. We would like to focus only on the dimensions/spaces that are closest to those used in auditory cortical processing. However, for most species the relevant auditory parameters are unknown, making it difficult to choose either appropriate basis functions or dimensions. One way to address this issue is by developing adaptive models with constrained inputs and constrained learning abilities. The feature decompositions learned by these models can then be compared with those observed in cortex. For example, Olshausen and Field [23,24] have developed unsupervised learning algorithms that find linear codes for natural visual scenes, given the constraints that these codes are sparse and statistically independent. The codes generated by their algorithms decompose images in ways similar to simple cells in visual cortex and wavelet transforms. Applying these algorithms to natural acoustic scenes and/or species-typical vocalizations may provide insights into which chirplet spaces are most applicable.

Olshausen and Fields' [23,24] adaptive image decomposition techniques are limited in that they do not account for coding and recognition of patterns that have been translated, rotated, or scaled; such coding is intrinsic to the chirplet transform. Their approach also does not incorporate the topographic feature decomposition typical of cortical processing. Kohonen [13–15] has developed a neural network, called an adaptive subspace self-organizing map, that addresses these limitations. Individual units in the self-organizing map (which are themselves composed of multiple computational neurons) learn to represent sets of input patterns that fall within a particular subspace. This network can learn to encode simple transformations (e.g., translation), and organizes such transformation “detectors” topographically. Interestingly, signal decompositions learned by this neural network have also been found to be comparable to both wavelet and visual cortical decomposition [13].

In our framework, each unit in an adaptive subspace self-organizing map can be viewed as representing a dimension within a chirplet subspace (given a particular set

of chirplet basis functions). Sets of units that share common bases can be considered to be analogous to a cortical field. Other wavelet-based self-organizing maps (e.g., see [6,9]) can also potentially be used to characterize auditory cortical parameter spaces.

The major obstacle blocking further development of this theoretical framework is the limited information available about the response properties of populations of auditory cortical neurons. Most attempts at characterizing the sensitivities of auditory cortex have looked at how individual neurons in primary auditory cortex respond to impoverished acoustic stimuli. Detailed descriptions of spectrotemporal response sensitivities have only recently begun to be reported [16,34]. Until such data are collected from a variety of species, it will be difficult to assess how effective our approach is at modeling encoding of acoustic events in mammalian cortices.

### 3. Conclusion

In this paper, we described a model of auditory cortical processing that more accurately reflects the complexity, variability, and flexibility seen in mammals. This model maps an overcomplete, acoustic signal decomposition onto a topographically organized, unsupervised neural network.

Our approach differs from previous approaches in that we start with an over-specified auditory parameter space, and attempt to reduce this space to reflect species-specific response sensitivities. Additionally, because our model is adaptive, it can be used to investigate changes in response sensitivities induced by experience (see also [2]).

The adaptive chirplet framework suggests new experimental directions for describing auditory cortical sensitivities. For example, measurements of experience-dependent changes in response sensitivities could be used to identify “paths of least resistance” in auditory parameter space. Such preferred trajectories could provide important clues about constraints on cortical sound decomposition and the chirplet bases/dimensions that best describe this process.

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